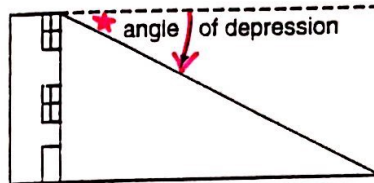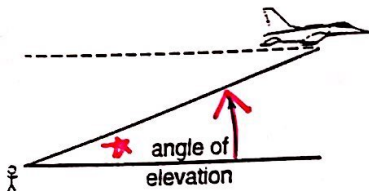# Study Guide 8-5

Angles of Elevation and Depression

Many problems in daily life can be solved by using trigonometry. Often such problems involve an **angle of elevation** or an **angle of depression**.

angle of depression

Note:
Angle of Elevation = Angle of Depression

Example: The angle of elevation from point A to the top of a cliff is 38°. If point A is 80 feet from the base of the cliff, how high is the cliff?
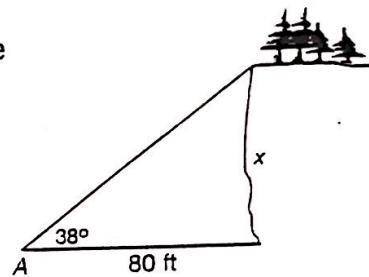
Let x represent the height of the cliff.
Then $\tan 38° = \frac{x}{80}$.

$80 \tan 38° = x$

x

38°

A 80 ft

Use a calculator set for the degree mode to find x.
ENTER: 80 ⊠ 38 TAN ⊟ 62.502850
The cliff is about 63 feet high.

Solve each problem. Round measures of segments to the nearest hundredth and measures of angles to the nearest degree.

1. From the top of a tower, the angle of depression to a stake on the ground is 72°. The top of the tower is 80 feet above ground. How far is the stake from the foot of the tower?

Sketch:

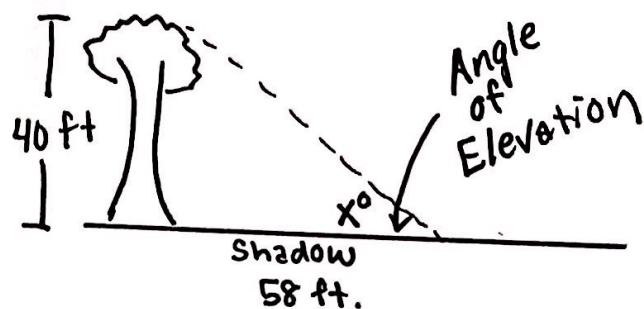Angle of Depression

80ft

Tower

72°

72°

X

Stake
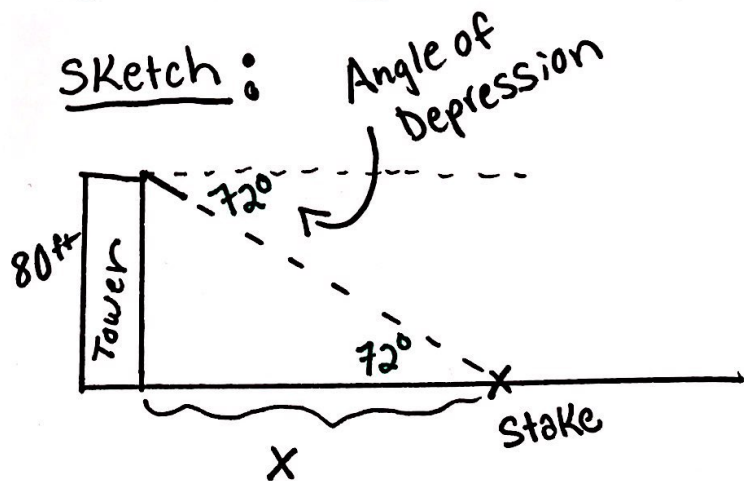
SOH CAH TOA

$\tan 72° = \frac{80}{x}$

$x \tan 72° = \frac{80}{x}(x)$

$x = \frac{80}{\tan 72°} \approx \boxed{25.99 \text{ ft}}$

2. A tree 40 feet high casts a shadow 58 feet long. Find the measure of the angle of elevation of the sun.
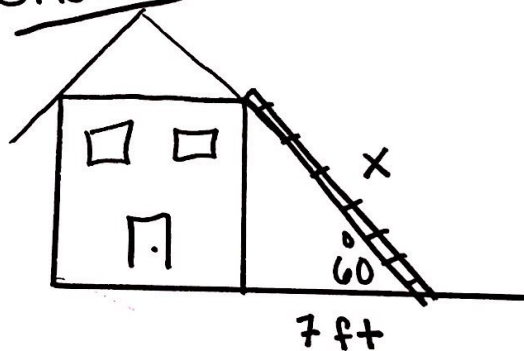
Sketch:

SOH CAH T͟O͟A͟

$$\text{Tan } x° = \frac{40}{58}$$

$$\text{Tan}^{-1}(\text{Tan } x°) = \text{Tan}^{-1}\left(\frac{40}{58}\right)$$

$$x° = \text{Tan}^{-1}\left(\frac{40}{58}\right)$$

$$\approx \boxed{34.59°}$$

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3. A ladder leaning against a house makes an angle of 60° with the ground. The foot of the ladder is 7 feet from the foundation of the house. How long is the ladder?

Sketch:

SOH C͟A͟H͟ TOA

$$\text{Cos } 60° = \frac{7}{x}$$

$$(x)\text{ Cos } 60° = \frac{7}{x}(x)$$

$$x \text{ Cos } 60° = 7$$

$$x = \frac{7}{\text{Cos } 60°}$$

$$\approx \boxed{14}$$